

### 433(3) : The Masses of Elementary Particle Beams

Consider the energy equation of m Hevy :

$$E^2 = c^2 p^2 + m(r) m^2 c^4 \quad (1)$$

where  $E$  is the relativistic energy,  $p$  the relativistic momentum, and  $m(r)$  the function that determines the nature of space through  $r$  is infinitesimal line element :

$$ds^2 = c^2 dt^2 = m(r) c^2 dt^2 - \frac{dr^2}{m(r)} - r^2 d\phi^2 \quad (2)$$

in plane polar coordinates, with generalization to other coordinate systems such as spherical polar. The quantization of eq. (1) takes place through :

$$p^\mu = i\hbar \partial^\mu \quad (3)$$

so :

$$\left( \frac{E}{c}, \underline{p} \right) = i\hbar \left( \frac{1}{c} \frac{\partial}{\partial t}, -\underline{\nabla} \right) \quad (4)$$

It follows that :

$$-\hbar^2 \frac{\partial^2 \psi}{\partial t^2} = -\hbar^2 c^2 \nabla^2 \psi + m(r) m^2 c^4 \psi \quad (5)$$

i.e

$$\left( \square + m(r) \left( \frac{mc}{\hbar} \right)^2 \right) \psi = 0 \quad (6)$$

where the d'Alembertian is :

$$\square = \frac{1}{c^2} \frac{\partial^2}{\partial t^2} - \nabla^2 \quad (7)$$

Therefore  $\psi$  is the wave corresponding to the

particle of mass  $m$ .

In general,  $\psi$  depends on  $r$  and  $t$  and is a moving wave. If  $\psi$  is considered to be a standing wave then:

$$\nabla^2 \psi = m(r) \left( \frac{mc}{\hbar} \right)^2 \psi \quad - (8)$$

and in this case  $\psi$  depends only on  $r$ . Now define the expectation value of  $m(r)$ :

$$\langle m(r) \rangle = \int \psi^* m(r) \psi d\tau \quad - (9)$$

Depending on the wave function  $\psi$  there are  $n$  values of  $\langle m(r) \rangle$ . There are  $n$  different particle masses. Using the Einstein/de Broglie equations:

$$\langle E \rangle = \hbar \omega \quad - (10)$$

and

$$\langle p \rangle = \hbar \kappa \quad - (11)$$

it follows that:

$$m^2 c^4 = \frac{\hbar^2 (\omega^2 - c^2 \kappa^2)}{\langle m(r) \rangle} \quad - (12)$$

So the particle masses are:

$$m^2 = \frac{\hbar^2 (\omega^2 - c^2 \kappa^2)}{\langle m(r) \rangle c^4} \quad - (13)$$

It follows that:

$$\langle n(r) \rangle \left( \frac{mc}{\hbar} \right)^2 = \left( \left( \frac{\omega}{c} \right)^2 - k^2 \right) - (14)$$

where

$$\langle n(r) \rangle = \int \psi^* n(r) \psi d\tau - (15)$$

From eq. (13):

$$E_0 = mc^2 = \hbar \left( \frac{\omega^2 - c^2 k^2}{\langle n(r) \rangle} \right)^{1/2} - (16)$$

The interaction between a proton and a neutron is mediated by several particles as follows:

Name	Particle	Antiparticle	$mc^2 / (\text{MeV})$
Pion	$\pi^+$	$\pi^-$	139.57018
Pion	$\pi^0$	$\pi^0$	134.9766
rho meson	$\rho^+$	$\rho^-$	775.11
rho meson	$\rho^0$	$\rho^0$	775.26
Omega meson	$\omega$	$\omega$	782.65

The rest energies of these several particles are defined by the expectation value (15), and the wave function is defined by eq. (6), where  $n(r)$  is the original  $n(r)$  function, which must be chosen to give the number of observed particles for a given nuclear interaction.