ON EXTENDING WHITTAKER'S THEORY, PART VI: PHOTONS WITHOUT FIELDS AND VECTOR POTENTIALS

We start with:

$$\mathbf{A} = \frac{1}{c}\dot{\mathbf{f}} - \nabla \times \mathbf{g}; \qquad \mathbf{B} = \nabla \times \mathbf{A}$$
 (1)

$$S = -c\nabla \times f - \dot{g}; \qquad E = -\nabla \times S. \tag{2}$$

If $\dot{f} = 0$ and $\nabla \times g = 0$ in eqn. (1a), then A and B vanish.

This means:

$$f = F(X, Y, Z)k \tag{3}$$

$$\mathbf{g} = G(t, \mathbf{Z})\mathbf{k} \tag{4}$$

with:

$$\Box F = \Box G = 0. \tag{5}$$

In the vicinity of the source, let:

$$F = A^{(0)} \left(X - iY \right) \tag{6}$$

$$G = \frac{G^{(0)}}{\sqrt{2}} e^{i(\omega t - \kappa Z)} \tag{7}$$

The propagating potential is:

$$g = Gk$$

The propagating scalar potential is:

$$\phi_L = \dot{G} = ic \frac{A^{(0)}}{\sqrt{2}} e^{i(\omega t - \kappa Z)}$$
(8)

It can be checked that:

$$\boldsymbol{E} = -\nabla \times \boldsymbol{S} = \boldsymbol{0} \tag{9}$$

as follows:

$$\nabla \times \mathbf{f} = A^{(0)} \begin{bmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ \frac{\partial}{\partial X} & \frac{\partial}{\partial Y} & \frac{\partial}{\partial Z} \\ X & -iY & 0 \end{bmatrix} = \mathbf{0}$$

An example of how fieldless G-waves can be generated is shown in Figure 1.

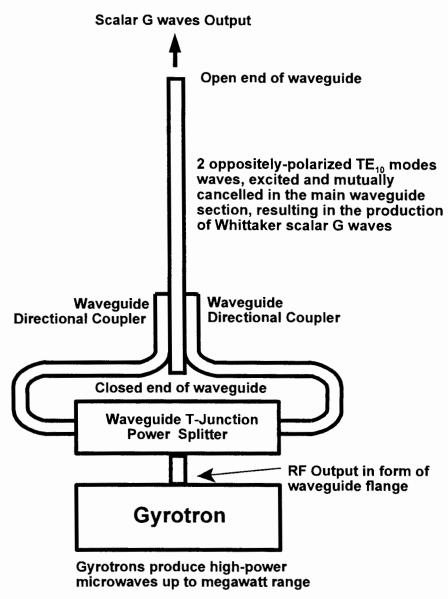


Figure 1: Practical conception for a source of scalar G waves.